Problem Solving • Multiplication and Division

Essential Question How can you use the strategy solve a simpler problem to help you solve a division problem?

UNLOCK the Problem REAL WORLD

Mark works at an animal shelter. To feed 9 dogs, Mark empties eight 18-ounce cans of dog food into a large bowl. If he divides the food equally among the dogs, how many ounces of food will each dog get?

Use the graphic organizer below to help you solve the problem.

Read the Problem Solve the Problem What do I need to find? • First, multiply to find the total number of I need to find ounces of dog food. 8 × 18 = • To find the number of ounces each dog What information do I need to use? gets, I'll need to divide. I need to use the number of _____, the 144 ÷ _____ = number of in each can, and the • To find the quotient, I break 144 into two number of dogs that need to be fed. simpler numbers that are easier to divide. $144 \div 9$ How will I use the information? (90 + ____) ÷ 9 I can to find the total number of ounces. Then I can solve a simpler problem to $(- \div 9) + (- - \div 9) =$ that total by 9.

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So, each dog gets _____ ounces of food.





Try Another Problem

Michelle is building shelves for her room. She has a plank 137 inches long that she wants to cut into 7 shelves of equal length. The plank has jagged ends, so she will start by cutting 2 inches off each end. How long will each shelf be?



Read the Problem	Solve the Problem
What do I need to find?	
What information do I need to use?	
How will I use the information?	
So, each shelf will be inches long.	Math Talk Explain how the strategy you used helped you solve the problem.

Name

Share and Show

 To make concrete mix, Monica pours 34 pounds of cement, 68 pounds of sand, 14 pounds of small pebbles, and 19 pounds of large pebbles into a large wheelbarrow. If she pours the mixture into 9 equalsize bags, how much will each bag weigh?

First, find the total weight of the mixture.

Then, divide the total by the number of bags. Break the total into two simpler numbers to make the division easier, if necessary.

Finally, find the quotient and solve the problem.

So, each bag will weigh _____ pounds.

- **2. What if** Monica pours the mixture into 5 equal-size bags? How much will each bag weigh?
- 3. Taylor is building doghouses to sell. Each doghouse requires 3 full sheets of plywood which Taylor cuts into new shapes. The plywood is shipped in bundles of 14 full sheets. How many doghouses can Taylor make from 12 bundles of plywood?

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UNLOCK the Problem

Underline what you need to find.

Circle the numbers you need to use.



 4. Eileen is planting a garden. She has seeds for 60 tomato plants, 55 sweet corn plants, and 21 cucumber plants. She plants them in 8 rows, with the same number of plants in each row. How many seeds are planted in each row?

Model • Reason • Make Sense Choose a

Act It Out

STRATEGY

Draw a Diagram

On Your Own...

- **5.** Starting on day 1 with 1 jumping jack, Keith doubles the number of jumping jacks he does every day. How many jumping jacks will Keith do on day 10?
- 6. Starting in the blue square, in how many different ways can you draw a line that passes through every square without picking up your pencil or crossing a line you've already drawn? Show the ways.



- 7. On April 11, Millie bought a lawn mower with a 50-day guarantee. If the guarantee begins on the date of purchase, what is the first day on which the mower will no longer be guaranteed?
- 8. A classroom bulletin board is 7 feet by 4 feet. If there is a picture of a student every 6 inches along the edge, including one in each corner, how many pictures are on the bulletin board?
- 9. Dave wants to make a stone walkway. The rectangular walkway is 4 feet wide and 12 feet long. Each 2 foot by 2 foot stone covers an area of 4 square feet. How many stones will Dave need to make his walkway?
- **10. Test Prep** Dee has 112 minutes of recording time. How many 4-minute songs can she record?

A 28	(C) 18
\bigcirc	\sim

Name ___

Numerical Expressions

Essential Question How can you use a numerical expression to describe a situation?

UNLOCK the Problem TREAL

A **numerical expression** is a mathematical phrase that has numbers and operation signs but does not have an equal sign.

Tyler caught 15 small bass, and his dad caught 12 small bass in the Memorial Bass Tourney in Tidioute, PA. Write a numerical expression to represent how many fish they caught in all.

Choose which operation to use.

You need to join groups of different sizes, so use addition.

15 small bass	plus	12 small bass
\downarrow	\downarrow	\downarrow
15	+	12

WORLD



So, 15 + 12 represents how many fish they caught in all.

Example 1 Write an expression to match the words.

Addition

Emma has 11 fish in her aquarium. She buys 4 more fish.

fish ↓	plus ↓	more fish \downarrow
11	+	4

G Multiplication

Karla buys 5 books. Each book costs \$3.

books	multiplied	cost per
	by	book
\downarrow	\downarrow	\downarrow
	×	

B Subtraction

Lucia has 128 stamps. She uses 38 stamps on party invitations.

stamps minus stamps used ↓ ↓ ↓ 128 - ____ Division

Four players share 52 cards equally.

divided	players
by	
\checkmark	\downarrow
÷	
	divided by ↓ ÷

MATHEMATICAL PRACTICES

expression represents.

Expressions with Parentheses The meaning of the words in a problem will tell you where to place the parentheses in an expression.

Example 2 Which expression matcher the meaning of the words? Doug went fishing for 3 days. Each day he put \$15 in At the end of each day, he had \$5 left. How much me Doug spend by the end of the trip?	 • Underline the events for each day. • Circle the number of days these events happened.
Think: Each day he took \$15 and had \$5 left. He did this for (\$15 − \$5) ← Think: What expression can you write to show how much money Doug spends in one day?	or 3 days. 3 × (\$15 − \$5) ← Think: What expression can you write to show how much money Doug spends in three days?
Example 3 Which problem matches the expression \$20 – (\$12 + \$3)?	MATHEMATICAL PRACTICES Math Talk Explain how the expression of what Doug spent in three days compares to the expression of what he spent in one day?
Kim has \$20 to spend for her fishing trip. She spends \$12 on a fishing pole. Then she finds \$3. How much money does Kim have now?	Kim has \$20 to spend for her fishing trip. She spends \$12 on a fishing pole and \$3 on bait. How much money does Kim have now?
List the events in order.	List the events in order.
First: Kim has \$20.	First: Kim has \$20.
Next:	Next:
Then:	Then:
Do these words	Do these words
match the expression?	match the expression?



Circle the expression that matches the words.

1. Teri had 18 worms. She gave 4 worms to Susie and 3 worms to Jamie.

```
(18 - 4) + 3 18 - (4 + 3)
```

 Rick had \$8. He then worked 4 hours for \$5 each hour.

 $(\$8 + 4) \times \5

 $8 + (4 \times 5)$

Nan	ne		_
Writ	e an expression to match the words.		
3.	Greg drives 26 miles on Monday and 90 miles on Tuesday.	ð 4.	Lynda has 27 fewer fish than Jack. Jack has 80 fish.
Writ	e words to match the expression.		
5.	34 - 17	 6.	$6 \times (12 - 4)$
			MATHEMATICAL PRACTICES Math Talk Is $4 \times 8 = 32$ an expression? Explain why or why not
On Write	e an expression to match the words.	••••	expression: Explain why of why not.
7.	José shared 12 party favors equally among 6 friends.	8.	Braden has 14 baseball cards. He finds 5 more baseball cards.
9.	Isabelle bought 12 bottles of water at \$2 each.	10.	Monique had \$20. She spent \$5 on lunch and \$10 at the bookstore.
Writ	e words to match the expression.	- 1	
11.	36 ÷ 9	12.	35 - (16 + 11)
Drav	w a line to match the expression with the w	ords.	
13.	Fred catches 25 fish. Then he releases • 10 fish and catches 8 more.		• 3 × (15 – 6)
	Nick has 25 pens. He gives 10 pens to one friend and 8 pens to another friend.		• 15 - 6
	Jan catches 15 fish and lets 6 fish go. •		• $25 - (10 + 8)$
	Libby catches 15 fish and lets 6 fish go for three days in a row.		• (25 - 10) + 8

Problem Solving REAL WORLD

Use the rule and the table for 14.

- **14.** Write a numerical expression to represent the total number of lemon tetras that could be in a 20-gallon aquarium.
- **15.** Write a word problem for an expression that is three times as great as (15 + 7). Then write the expression.

Aquarium Fish	
Type of Fish	Length (in inches)
Lemon Tetra	2
Strawberry Tetra	3
Giant Danio	5
Tiger Barb	3
Swordtail	5

The rule for the number of fish in an aquarium is to allow 1 gallon of water for each inch of length.

SHOW YOUR WORK

16. What's the Question? Lu has 3 swordtails in her aquarium. She buys 2 more swordtails.

17. Tammy gives 45 stamps to her 9 friends. She shares them equally among her friends. Write an expression to match the words. How many stamps does each friend get?

- **18.** Test Prep Josh has 3 fish in each of 5 buckets. Then he releases 4 fish. Which expression matches the words?
 - (A) $(3 \times 4) 5$
 - **B** $(5 \times 4) 3$
 - **(C)** $(5 \times 3) 4$
 - **D** $(5-3) \times 4$

Name _

Evaluate Numerical Expressions

Essential Question In what order must operations be evaluated to find the solution to a problem?

CONNECT Remember that a numerical expression is a mathematical phrase that uses only numbers and operation symbols.

 $72 \div 9 + 16$ (24 - 15) + 32 $(5-2) \times 7$

To evaluate, or find the value of, a numerical expression with more than one operation, you must follow rules called the order of operations. The order of operations tells you in what order you should evaluate an expression.

UNLOCK the Problem REAL WORLD

A cake recipe calls for 4 cups of flour and 2 cups of sugar. To triple the recipe, how many cups of flour and sugar are needed in all?

Evaluate $3 \times 4 + 3 \times 2$ to find the total number of cups.

- A Heather did not follow the order of operations correctly.
- B Follow the order of operations by multiplying first and then adding.



	Name
0	3×4+3×2
0	

So, _____ cups of flour and sugar are needed.

ALGEBRA Lesson 1.11

Order of Operations

- 1. Perform operations in parentheses.
- 2. Multiply and divide from left to right.
- 3. Add and subtract from left to right.

Evaluate Expressions with Parentheses To evaluate an expression with parentheses, follow the order of operations. Perform the operations in parentheses first. Multiply from left to right. Then add and subtract from left to right.

🚹 Example

Each batch of cupcakes Lena makes uses 3 cups of flour, 1 cup of milk, and 2 cups of sugar. Lena wants to make 5 batches of cupcakes. How many cups of flour, milk, and sugar will she need in all?

Write the expression.

5 × (3 + 1 + 2)

First, perform the operations in parentheses. $5 \times ($ ____)

Then multiply.

So, Lena will use _____ cups of flour, milk, and sugar in all.

 What if Lena makes 4 batches? Will this change the numerical expression? Explain.

Try This! Rewrite the expression with parentheses to equal the given value.

▲ 6 + 12 × 8 - 3; value	e: 141
-------------------------	--------

- Evaluate the expression without the parentheses.
- Try placing the parentheses in the expression so the value is 141.

Think: Will the placement of the parentheses increase or decrease the value of the expression?

B 5 + 28 ÷ 7 − 4; value: 11

- Evaluate the expression without the parentheses.
- Try placing the parentheses in the expression so that the value is 11.

Think: Will the placement of the parentheses increase or decrease the value of the expression?

• Use order of operations to check your work.

• Use order of operations to check your work.

 $6+12\ \times 8-3$

 $5 + 28 \div 7 - 4$

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Name		
Share and Sho Evaluate the numerical e	xpression.	
1. 10 + 36 ÷ 9	3. $9 - (3 \times 2) + 8$	
Think: I need to divide fi	rst.	
	Math TalkMath TalkRaina evaluated the expression $5 \times 2 + 2$ by adding first and then multiplying. Will her answer be correct? Explain.	
Evaluate the numerical e	xpression.	
4. (4 + 49) - 4 × 10	5. $5 + 17 - 100 \div 5$ 6. $36 - (8 + 5)$ 7. $125 - (68 + 7)$	
$(4 \times 6) = 12$	9 $3 \times (22 - 2)$ 10 $23 \pm (16 - 7)$ 11 $(25 - 4) \pm 3$	
6. (4 × 0) 12	5. $5 \land (22 \ 2)$ 10. $25 \land (10 \ 7)$ 11. $(25 \ 4) \land 5$	
Rewrite the expression w	ith parentheses to equal the given value.	
12. 100 - 30 ÷ 5 value: 14	13. $12 + 17 - 3 \times 2$ 14. $9 + 5 \div 5 + 2$ value: 23 value: 2	

Model • Reason • Make Sense



- eats about 30 pounds of food each day. Which expression shows how many pounds of food 6 pandas eat in 3 days?
 - (A) $3 + (30 \times 6)$
 - **(B)** $3 \times (30 \times 6)$
 - (C) $(30 \times 6) \div 3$
 - **(D)** $(30 \times 6) 3$

- a value of 6?
 - (A) (6 ÷ 3) × 4 + 8 **(B)** $27 - 9 \div 3 \times (4 + 1)$ (C) $(18 + 12) \times 6 - 4$ **(D)** $71 - 5 \times (9 + 4)$

Name ____

Grouping Symbols

Essential Question In what order must operations be evaluated to find a solution when there are parentheses within parentheses?

UNLOCK the Problem

Mary's weekly allowance is \$8 and David's weekly allowance is \$5. Every week they each spend \$2 on lunch. Write a numerical expression to show how many weeks it will take them together to save enough money to buy a video game for \$45.

- Underline Mary's weekly allowance and how much she spends.
- Circle David's weekly allowance and how much he spends.

Use parentheses and brackets to write an expression.

You can use parentheses and brackets to group operations that go together. Operations in parentheses and brackets are performed first.

STEP 1 Write an expression to represent how much Mary and David save each week.

• How much money does Mary save each week?

Think: Each week Mary gets \$8 and spends \$2.



David save together each week?

STEP 2 Write an expression to represent how many weeks it will take Mary and David to save enough money for the video game.

• How many weeks will it take Mary and David to save enough for a video game?

Think: I can use brackets to group operations a second time. \$45 is divided by the total amount of money saved each week.

_____÷[_____]

How much money does David save each week?

Think: Each week David gets \$5 and spends \$2.

)

MATHEMATICAL PRACTICES

Math Talk Explain why brackets are placed around the part of the expression that represents the amount of money Mary and David save each week.

Evaluate Expressions with Grouping Symbols When evaluating an expression with different grouping symbols (parentheses, brackets, and braces), perform the operation in the innermost set of grouping symbols first, evaluating the expression from the inside out.

🚹 Example

John gets \$6 for his weekly allowance and spends \$4 of it. His sister Tina gets \$7 for her weekly allowance and spends \$3 of it. Their mother's birthday is in 4 weeks. If they spend the same amount each week, how much money can they save together in that time to buy her a present?

- Write the expression using parentheses and brackets.
- Perform the operations in the parentheses first.
- Next perform the operations in the brackets.
- Then multiply.

So, John and Tina will be able to save ______ for their mother's birthday present.

 What if only Tina saves any money? Will this change the numerical expression? Explain.

Try This! Follow the order of operations.

A $4 \times \{[(5-2) \times 3] + [(2+4) \times 2]\}$	
• Perform the operations in the parentheses.	4 × {[3 × 3] + [×]}
• Perform the operations in the brackets.	4 × {9 +}
• Perform the operations in the braces.	4 ×
Multiply.	
~	
B $32 \div \{[(3 \times 2) + 7] - [(6 - 4) + 7]\}$	
• Perform the operations in the parentheses.	32 ÷ {[+] – [+]}
• Perform the operations in the brackets.	32 ÷ {}
• Perform the operations in the braces.	32 ÷
• Divide.	





 $4 \times [(\$6 - \$4) + (\$7 - \$3)]$

4 × [_____ + ____]

4 × _____